

Appendix E

Tables for Prediction of Transport Properties

§E.1 Intermolecular force parameters and critical properties

§E.2 Functions for prediction of transport properties of gases at low densities

Table E.1 Lennard-Jones (6-12) Potential Parameters and Critical Properties

Substance	Molecular Weight <i>M</i>	Lennard-Jones parameters			Critical properties ^{a,b}				
		σ (Å)	ϵ/κ (K)	Ref.	T_c (K)	p_c (atm)	\tilde{V}_c (cm ³ /g-mole)	μ_c (g/cm ³ · s × 10 ⁶)	k_c (cal/cm ³ · s · K × 10 ⁶)
Light elements:									
H ₂	2.016	2.915	38.0	<i>a</i>	33.3	12.80	65.0	34.7	—
He	4.003	2.576	10.2	<i>a</i>	5.26	2.26	57.8	25.4	—
Noble gases:									
Ne	20.180	2.789	35.7	<i>a</i>	44.5	26.9	41.7	156.	79.2
Ar	39.948	3.432	122.4	<i>b</i>	150.7	48.0	75.2	264.	71.0
Kr	83.80	3.675	170.0	<i>b</i>	209.4	54.3	92.2	396.	49.4
Xe	131.29	4.009	234.7	<i>b</i>	289.8	58.0	118.8	490.	40.2
Simple polyatomic gases:									
Air	28.964 ⁱ	3.617	97.0	<i>a</i>	132.4 ⁱ	37.0 ⁱ	86.7 ⁱ	193.	90.8
N ₂	28.013	3.667	99.8	<i>b</i>	126.2	33.5	90.1	180.	86.8
O ₂	31.999	3.433	113.	<i>a</i>	154.4	49.7	74.4	250.	105.3
CO	28.010	3.590	110.	<i>a</i>	132.9	34.5	93.1	190.	86.5
CO ₂	44.010	3.996	190.	<i>a</i>	304.2	72.8	94.1	343.	122.
NO	30.006	3.470	119.	<i>a</i>	180.	64.	57.	258.	118.2
N ₂ O	44.012	3.879	220.	<i>a</i>	309.7	71.7	96.3	332.	131.
SO ₂	64.065	4.026	363.	<i>c</i>	430.7	77.8	122.	411.	98.6
F ₂	37.997	3.653	112.	<i>a</i>	—	—	—	—	—
Cl ₂	70.905	4.115	357.	<i>a</i>	417.	76.1	124.	420.	97.0
Br ₂	159.808	4.268	520.	<i>a</i>	584.	102.	144.	—	—
I ₂	253.809	4.982	550.	<i>a</i>	800.	—	—	—	—
Hydrocarbons:									
CH ₄	16.04	3.780	154.	<i>b</i>	191.1	45.8	98.7	159.	158.
CH=CH	26.04	4.114	212.	<i>d</i>	308.7	61.6	112.9	237.	—
CH ₂ =CH ₂	28.05	4.228	216.	<i>b</i>	282.4	50.0	124.	215.	—
C ₂ H ₆	30.07	4.388	232.	<i>b</i>	305.4	48.2	148.	210.	203.
CH ₃ C≡CH	40.06	4.742	261.	<i>d</i>	394.8	—	—	—	—
CH ₃ CH=CH ₂	42.08	4.766	275.	<i>b</i>	365.0	45.5	181.	233.	—
C ₃ H ₈	44.10	4.934	273.	<i>b</i>	369.8	41.9	200.	228.	—
<i>n</i> -C ₄ H ₁₀	58.12	5.604	304.	<i>b</i>	425.2	37.5	255.	239.	—

<i>i</i> -C ₄ H ₁₀	58.12	5.393	295.	<i>b</i>	408.1	36.0	263.	239.	—
<i>n</i> -C ₅ H ₁₂	72.15	5.850	326.	<i>b</i>	469.5	33.2	311.	238.	—
<i>i</i> -C ₃ H ₈	72.15	5.812	327.	<i>b</i>	460.4	33.7	306.	—	—
C(CH ₃) ₄	72.15	5.759	312.	<i>b</i>	433.8	31.6	303.	—	—
<i>n</i> -C ₆ H ₁₄	86.18	6.264	342.	<i>b</i>	507.3	29.7	370.	248.	—
<i>n</i> -C ₇ H ₁₆	100.20	6.663	352.	<i>b</i>	540.1	27.0	432.	254.	—
<i>n</i> -C ₈ H ₁₈	114.23	7.035	361.	<i>b</i>	568.7	24.5	492.	259.	—
<i>n</i> -C ₉ H ₂₀	128.26	7.463	351.	<i>b</i>	594.6	22.6	548.	265.	—
Cyclohexane	84.16	6.143	313.	<i>d</i>	553.	40.0	308.	284.	—
Benzene	78.11	5.443	387.	<i>b</i>	562.6	48.6	260.	312.	—
Other organic compounds:									
CH ₄	16.04	3.780	154.	<i>b</i>	191.1	45.8	98.7	159.	158.
CH ₃ Cl	50.49	4.151	355.	<i>c</i>	416.3	65.9	143.	338.	—
CH ₂ Cl ₂	84.93	4.748	398.	<i>c</i>	510.	60.	—	—	—
CHCl ₃	119.38	5.389	340.	<i>e</i>	536.6	54.	240.	410.	—
CCl ₄	153.82	5.947	323.	<i>e</i>	556.4	45.0	276.	413.	—
C ₂ N ₂	52.034	4.361	349.	<i>e</i>	400.	59.	—	—	—
COS	60.076	4.130	336.	<i>e</i>	378.	61.	—	—	—
CS ₂	76.143	4.483	467.	<i>e</i>	552.	78.	170.	404.	—
CCl ₂ F ₂	120.91	5.116	280.	<i>b</i>	384.7	39.6	218.	—	—

^a J. O. Hirschfelder, C. F. Curtiss, and R. B. Bird, *Molecular Theory of Gases and Liquids*, corrected printing with notes added, Wiley, New York (1964).

^b L. S. Tee, S. Gotoh, and W. E. Stewart, *Ind. Eng. Chem. Fundamentals*, **5**, 356–363 (1966). The values for benzene are from viscosity data on that substance. The values for other substances are computed from Correlation (iii) of the paper.

^c L. Monchick and E. A. Mason, *J. Chem. Phys.*, **35**, 1676–1697 (1961); parameters obtained from viscosity.

^d L. W. Flynn and G. Thodos, *AIChE Journal*, **8**, 362–365 (1962); parameters obtained from viscosity.

^e R. A. Svehla, *NASA Tech. Report R-132* (1962); parameters obtained from viscosity. This report provides extensive tables of Lennard-Jones parameters, heat capacities, and calculated transport properties.

^f Values of the critical constants for the pure substances are selected from K. A. Kobe and R. E. Lynn, Jr., *Chem. Rev.*, **52**, 117–236 (1962); *Amer. Petroleum Inst. Research Proj. 44*, Thermodynamics Research Center, Texas A&M University, College Station, Texas (1966); and *Thermodynamic Functions of Gases*, F. Din (editor), Vols. 1–3, Butterworths, London (1956, 1961, 1962).

^g Values of the critical viscosity are from O. A. Hougen and K. M. Watson, *Chemical Process Principles*, Vol. 3, Wiley, New York (1947), p. 873.

^h Values of the critical thermal conductivity are from E. J. Owens and G. Thodos, *AIChE Journal*, **3**, 454–461 (1957).

ⁱ For air, the molecular weight *M* and the pseudocritical properties have been computed from the average composition of dry air as given in COESA, *U.S. Standard Atmosphere 1976*, U.S. Government Printing Office, Washington, D.C. (1976).

Table E.2 Collision Integrals for Use with the Lennard-Jones (6-12) Potential for the Prediction of Transport Properties of Gases at Low Densities^{a,b,c}

$\kappa T/\varepsilon$ or $\kappa T/\varepsilon_{AB}$	$\Omega_\mu = \Omega_k$ (for viscosity and thermal conductivity)	$\Omega_{\mathcal{D},AB}$ (for diffusivity)	$\kappa T/\varepsilon$ or $\kappa T/\varepsilon_{AB}$	$\Omega_\mu = \Omega_k$ (for viscosity and thermal conductivity)	$\Omega_{\mathcal{D},AB}$ (for diffusivity)
0.30	2.840	2.649	2.7	1.0691	0.9782
0.35	2.676	2.468	2.8	1.0583	0.9682
0.40	2.531	2.314	2.9	1.0482	0.9588
0.45	2.401	2.182	3.0	1.0388	0.9500
0.50	2.284	2.066	3.1	1.0300	0.9418
0.55	2.178	1.965	3.2	1.0217	0.9340
0.60	2.084	1.877	3.3	1.0139	0.9267
0.65	1.999	1.799	3.4	1.0066	0.9197
0.70	1.922	1.729	3.5	0.9996	0.9131
0.75	1.853	1.667	3.6	0.9931	0.9068
0.80	1.790	1.612	3.7	0.9868	0.9008
0.85	1.734	1.562	3.8	0.9809	0.8952
0.90	1.682	1.517	3.9	0.9753	0.8897
0.95	1.636	1.477	4.0	0.9699	0.8845
1.00	1.593	1.440	4.1	0.9647	0.8796
1.05	1.554	1.406	4.2	0.9598	0.8748
1.10	1.518	1.375	4.3	0.9551	0.8703
1.15	1.485	1.347	4.4	0.9506	0.8659
1.20	1.455	1.320	4.5	0.9462	0.8617
1.25	1.427	1.296	4.6	0.9420	0.8576
1.30	1.401	1.274	4.7	0.9380	0.8537
1.35	1.377	1.253	4.8	0.9341	0.8499
1.40	1.355	1.234	4.9	0.9304	0.8463
1.45	1.334	1.216	5.0	0.9268	0.8428
1.50	1.315	1.199	6.0	0.8962	0.8129
1.55	1.297	1.183	7.0	0.8727	0.7898
1.60	1.280	1.168	8.0	0.8538	0.7711
1.65	1.264	1.154	9.0	0.8380	0.7555
1.70	1.249	1.141	10.0	0.8244	0.7422
1.75	1.235	1.128	12.0	0.8018	0.7202
1.80	1.222	1.117	14.0	0.7836	0.7025
1.85	1.209	1.105	16.0	0.7683	0.6878
1.90	1.198	1.095	18.0	0.7552	0.6751
1.95	1.186	1.085	20.0	0.7436	0.6640
2.00	1.176	1.075	25.0	0.7198	0.6414
2.10	1.156	1.058	30.0	0.7010	0.6235
2.20	1.138	1.042	35.0	0.6854	0.6088
2.30	1.122	1.027	40.0	0.6723	0.5964
2.40	1.107	1.013	50.0	0.6510	0.5763
2.50	1.0933	1.0006	75.0	0.6140	0.5415
2.60	1.0807	0.9890	100.0	0.5887	0.5180

^a The values in this table, applicable for the Lennard-Jones (6-12) potential, are interpolated from the results of L. Monchick and E. A. Mason, *J. Chem. Phys.*, **35**, 1676-1697 (1961). The Monchick-Mason table is believed to be slightly better than the earlier table by J. O. Hirschfelder, R. B. Bird, and E. L. Spatz, *J. Chem. Phys.*, **16**, 968-981 (1948).

^b This table has been extended to lower temperatures by C. F. Curtiss, *J. Chem. Phys.*, **97**, 7679-7686 (1992). Curtiss showed that at low temperatures, the Boltzmann equation needs to be modified to take into account "orbiting pairs" of molecules. Only by making this modification is it possible to get a smooth transition from quantum to classical behavior. The deviations are appreciable below dimensionless temperatures of 0.30.

^c The collision integrals have been curve-fitted by P. D. Neufeld, A. R. Jansen, and R. A. Aziz, *J. Chem. Phys.*, **57**, 1100-1102 (1972), as follows:

$$\Omega_\mu = \Omega_k = \frac{1.16145}{T^{*0.14874}} + \frac{0.52487}{\exp(0.77320T^*)} + \frac{2.16178}{\exp(2.43787T^*)} \quad (\text{E.2-1})$$

$$\Omega_{\mathcal{D},AB} = \frac{1.06036}{T^{*0.15610}} + \frac{0.19300}{\exp(0.47635T^*)} + \frac{1.03587}{\exp(1.52996T^*)} + \frac{1.76474}{\exp(3.89411T^*)} \quad (\text{E.2-2})$$

where $T^* = \kappa T/\varepsilon$.